JEE (Main)-2025 Phase-1

22/01/25_Morning

(Mathematics, Physics and Chemistry)

IMPORTANT INSTRUCTIONS:

(1) The test is of 3 hours duration.
(2) This test paper consists of 75 questions. Each subject (MPC) has 25 questions. The maximum marks are 300 .
(3) This question paper contains Three Parts. Part-A is Physics, Part-B is Chemistry and Part-C is Mathematics. Each part has only two sections: Section-A and Section-B.
(4) Section - A : Attempt all questions.
(5) Section - B : Attempt all questions.
(6) Section - A (01-20) contains 20 multiple choice questions which have only one correct answer. Each question carries + 4 marks for correct answer and – 1 mark for wrong answer.
(7) Section-B(21-25) contains 5 Numerical value based questions. The answer to each question should be rounded off to the nearest integer. Each question carries + 4 marks for correct answer and -1 mark for wrong answer.

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

1. From all the English alphabets, five letters are chosen and are arranged in alphabetical order. The total number of ways, in which the middle letter is ' M ', is:
   (1) 4356
   (2) 6084
   (3) 14950
   (4) 5148

2. Using the principal values of the inverse trigonometric functions, the sum of the maximum and the minimum values of $16\left(\left(\sec^{-1} x\right)^2+\left(\operatorname{cosec}^{-1} x\right)^2\right)$ is:

(1) $18\pi^2$
(2) $31\pi^2$
(3) $24\pi^2$
(4) $22\pi^2$

3. The number of non-empty equivalence relations on the set {1,2,3} is:
(1) 5
(2) 7
(3) 4
(4) 6

4. Let

$$L_1: \frac{x-1}{2}=\frac{y-2}{3}=\frac{z-3}{4}$$

and $L_2: \frac{x-2}{3}=\frac{y-4}{4}=\frac{z-5}{5}$ be two lines. Then which of the following points lies on the line of the shortest distance between L_1 and L_2 ?

(1) $\left(\frac{8}{3},-1,\frac{1}{3}\right)$
(2) $\left(2,3,\frac{1}{3}\right)$
(3) $\left(\frac{14}{3},-3,\frac{22}{3}\right)$
(4) $\left(-\frac{5}{3},-7,1\right)$

5. Let the foci of a hyperbola be (1,14) and (1, – 12). If it passes through the point (1,6), then the length of its latus-rectum is:
(1) $\frac{25}{6}$
(2) $\frac{288}{5}$
(3) $\frac{144}{5}$
(4) $\frac{24}{5}$

6. A coin is tossed three times. Let X denote the number of times a tail follows a head. If μ and σ^2 denote the mean and variance of X, then the value of $64\left(\mu+\sigma^2\right)$ is:
(1) 48
(2) 32
(3) 64
(4) 51

7. Let the triangle PQR be the image of the triangle with vertices (1,3),(3,1) and (2,4) in the line $x + 2y = 2$. If the centroid of $\triangle PQR$ is the point (α,β), then $15(\alpha - \beta)$ is equal to:
(1) 19
(2) 24
(3) 22
(4) 21

8. Let $f(x)$ be a real differentiable function such that $f(0) = 1$ and $f(x + y) = f(x)f'(y) + f'(x)f(y)$ for all $x,y \in R$.
Then $\sum_{n=1}^{100} \log_e f(n)$ is equal to:
(1) 2406
(2) 2384
(3) 2525
(4) 5220

9. The area of the region, inside the circle $(x - 2\sqrt{3})^2 + y^2 = 12$ and outside the parabola $y^2 = 2\sqrt{3}x$ is:
(1) $3\pi - 8$
(2) $3\pi + 8$
(3) $6\pi - 16$
(4) $6\pi - 8$

10. Let $a_1,a_2,a_3,\ldots$ be a G.P. of increasing positive terms. If $a_1a_5 = 28$ and $a_2 + a_4 = 29$, then a_6 is equal to:
(1) 628
(2) 812
(3) 526
(4) 784

11. Let z_1,z_2 and z_3 be three complex numbers on the circle $|z| = 1$ with $\arg(z_1) = \frac{-\pi}{4}$, $\arg(z_2) = 0$ and $\arg(z_3) = \frac{\pi}{4}$. If $\left|\overline{z_1z_2} + \overline{z_2z_3} + \overline{z_3z_1}\right|^2 = \alpha + \beta\sqrt{2}, \alpha,\beta \in Z$, then the value of $\alpha^2 + \beta^2$ is:
(1) 31
(2) 29
(3) 41
(4) 24

12. Let $f:R \to R$ be a twice differentiable function such that $f(x + y) = f(x)f(y)$ for all $x,y \in R$. If $f'(0) = 4a$ and f satisfies $f'(x) - 3af'(x) - f(x) = 0, a > 0$, then the area of the region $R = \{(x,y) \mid 0 \le y \le f(ax), 0 \le x \le 2\}$ is:
(1) $e^2 - 1$
(2) $e^4 - 1$
(3) $e^2 + 1$
(4) $e^4 + 1$

13. Let $x = x(y)$ be the solution of the differential equation $y^2dx + \left(x - \frac{1}{y}\right)dy = 0$. If $x(1) = 1$, then $x\left(\frac{1}{2}\right)$ is
(1) $\frac{3}{2} + e$
(2) $3 - e$
(3) $3 + e$
(4) $\frac{1}{2} + e$

14. Two balls are selected at random one by one without replacement from a bag containing 4 white and 6 black balls. If the probability that the first selected ball is black, given that the second selected ball is also black, is $\frac{m}{n}$, where $\gcd(m,n) = 1$, then $m + n$ is equal to
(1) 13
(2) 11
(3) 14
(4) 4

15. Let the parabola $y = x^2 + px - 3$, meet the coordinate axes at the points P,Q and R. If the circle C with centre at $(-1, -1)$ passes through the points P,Q and R, then the area of $\triangle PQR$ is
(1) 5
(2) 4
(3) 7
(4) 6

16. A circle C of radius 2 lies in the second quadrant and touches both the coordinate axes. Let r be the radius of a circle that has centre at the point (2,5) and intersects the circle C at exactly two points. If the set of all possible values of r is the interval (α,β), then $3\beta - 2\alpha$ is equal to:
(1) 12
(2) 14
(3) 15
(4) 10

17. If $\sum_{r=1}^{n} T_r = \frac{(2n-1)(2n+1)(2n+3)(2n+5)}{64}$, then $\lim_{n\to\infty} \sum_{r=1}^{n} \left(\frac{1}{T_r}\right)$ is equal to
(1) 0
(2) 1
(3) $\frac{1}{3}$
(4) $\frac{2}{3}$

18. Let $A = \{1,2,3,\ldots,10\}$ and $B = \left\{\frac{m}{n} : m,n \in A, m < n \text{ and } \gcd(m,n) = 1\right\}$. Then $n(B)$ is equal to
(1) 36
(2) 31

(3) 29
(4) 37

19. The product of all solutions of the equation $e^{5(\log_e x)^2+3} = x^8, x > 0$, is
(1) $e^{\frac{6}{5}}$
(2) e
(3) $e^{\frac{8}{5}}$
(4) e^2

20. Let for $f(x) = 7\tan^8 x + 7\tan^6 x - 3\tan^4 x - 3\tan^2 x$, $I_1 = \int_0^{\frac{\pi}{4}} f(x)dx$ and $I_2 = \int_0^{\frac{\pi}{4}} xf(x)dx$. Then $7I_1 + 12/2$ is equal to
(1) π
(2) 2π
(3) 1
(4) 2

SECTION - B

Numerical Value Type Questions: This section contains 5Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Let $\vec{c}$ be the projection vector of $\vec{b} = \lambda\hat{i} + 4\hat{k}, \lambda > 0$, on the vector $\vec{a} = \hat{i} + 2\hat{j} + 2\hat{k}$. If $|\vec{a} + \vec{c}| = 7$, then the area of the parallelogram formed by the vectors $\vec{b}$ and $\vec{c}$ is ____

22. If $\sum_{r=0}^{5} \frac{^{11}C_{2r+1}}{2r+2} = \frac{m}{n}, gcd(m,n) = 1$, then $m - n$ is equal to ____ .

23. Let the function,
$f(x) = \begin{cases} -3ax^2 - 2, & x < 1 \\ a^2 + bx, & x \geq 1 \end{cases}$
be differentiable for all $x \in R$, where $a > 1, b \in R$. If the area of the region enclosed by $y = f(x)$ and the line $y = -20$ is $\alpha + \beta\sqrt{3}, \alpha, \beta \in Z$, then the value of $\alpha + \beta$ is ____ .

24. Let $L_1: \frac{x-1}{3} = \frac{y-1}{-1} = \frac{z+1}{0}$ and $L_2: \frac{x-2}{2} = \frac{y}{0} = \frac{z+4}{\alpha}, \alpha \in R$, be two lines, which intersect at the point B. If P is the foot of perpendicular from the point $A(1,1,-1)$ and L_2, then the value of $26\alpha(PB)^2$ is

25. Let A be a square matrix of order 3 such that $\det(A) = -2$ and $\det(3\text{adj}(-6\text{adj}(3A))) = 2^{m+n} \cdot 3^{mn}$, $m > n$. Then $4m + 2n$ is equal to ____ .

PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

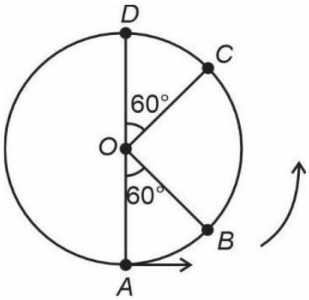
Choose the correct answer :

26. An electron is made to enter symmetrically between two parallel and equally but oppositely charged metal plates, each of 10 cm length. The electron emerge out of the electric field region with a horizontal component of velocity 10^6 m/s. If the magnitude of the electric field between the plates is 9.1 V/cm, then the vertical component of velocity of electron is
(mass of electron = 9.1×10^{-31} kg and charge of electron = 1.6×10^{-19}C)
(1) 0
(2) 16×10^6 m/s
(3) 16×10^4 m/s
(4) 1×10^6 m/s

27. An amount of ice of mass 10^{-3} kg and temperature – 10°C is transformed to vapour of temperature 110°C by applying heat. The total amount of work required for this conversion is, (Take, specific heat of ice = 2100Jkg^{-1} K^{-1}, specific heat of water 4180Jkg^{-1} K^{-1}, specific heat of steam = 1920Jkg^{-1} K^{-1}, Latent heat of ice = 3.35 $\times 10^5$Jkg^{-1} and Latent heat of steam = 2.25×10^6Jkg^{-1})
(1) 3022 J
(2) 3043 J
(3) 3024 J
(4) 3003 J

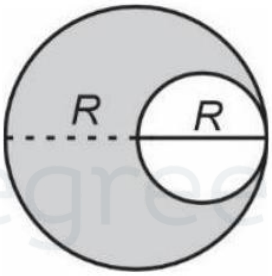
28. If B is magnetic field and μ_0 is permeability of free space, then the dimensions of (B/μ_0) is
(1) $ML^2T^{-2}A^{-1}$
(2) L^{-1} A
(3) LT^{-2} A^{-1}
(4) $MT^{-2}A^{-1}$

29. A bob of mass m is suspended at a point O by a light string of length I and left to perform vertical motion (circular) as shown in figure. Initially, by applying horizontal velocity v_0 at the point ' A ', the string becomes slack when, the bob reaches at the point ' D '. The ratio of the kinetic energy of the bob at the point B and C is ____ .



(1) 1
(2) 3
(3) 4
(4) 2

30. A uniform circular disc of radius ' R ' and mass ' M ' is rotating about an axis perpendicular to its plane and passing through its centre. A small circular part of radius $R/2$ is removed from the original disc as shown in the figure. Find the moment of inertia of the remaining part of the original disc about the axis as given above.



(1) $\frac{7}{32}MR^2$
(2) $\frac{17}{32}MR^2$
(3) $\frac{13}{32}MR^2$
(4) $\frac{9}{32}MR^2$

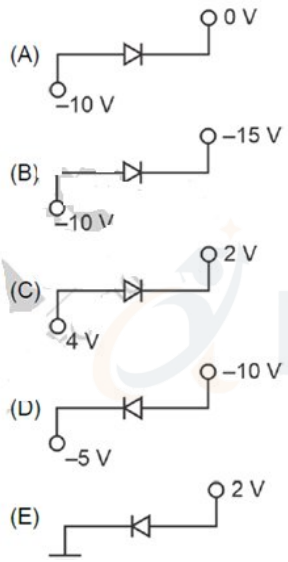
31. A parallel-plate capacitor of capacitance 40μ F is connected to a 100 V power supply. Now the intermediate space between the plates is filled with a dielectric material of dielectric constant K = 2. Due to the introduction of dielectric material, the extra charge and the change in the electrostatic energy in the capacitor, respectively, are
(1) 2 mC and 0.4 J
(2) 8 mC and 2.0 J
(3) 4 mC and 0.2 J
(4) 2 mC and 0.2 J

32. The work functions of cesium (Cs) and lithium (Li) metals are 1.9 eV and 2.5 eV , respectively. If we incident a light of wavelength 550 nm on these two metal surfaces, then photo-electric effect is possible for the case of
(1) Neither Cs nor Li
(2) Both Cs and Li

(3) Cs only
(4) Li only

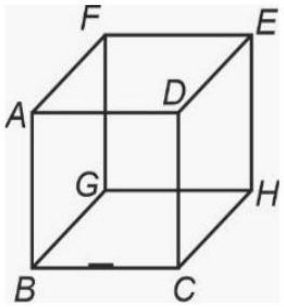
33. An electron in the ground state of the hydrogen atom has the orbital radius of 5.3×10^{-11} m while that for the electron in third excited state is 8.48×10^{-10} m. The ratio of the de Broglie wavelengths of electron in the ground state to that in the excited state is
(1) 4
(2) 16
(3) 3
(4) 9

34. Which of the following circuits represents a forward biased diode?



Choose the correct answer from the options given below:
(1) (B), (D) and (E) only
(2) (A) and (D) only
(3) (C) and (E) only
(4) (B), (C) and (E) only

35. A line charge of length $\frac{'a}{2}$ is kept at the center of an edge BC of a cube ABCDEFGH having edge length ' a ' as shown in the figure. If the density of line charge is λC per unit length, then the total electric flux through all the faces of the cube will be ____ . (Take, ε_0 as the free space permittivity)



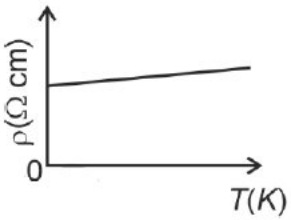
(1) $\frac{\lambda a}{16\varepsilon_0}$
(2) $\frac{\lambda a}{2\varepsilon_0}$
(3) $\frac{\lambda a}{4\varepsilon_0}$
(4) $\frac{\lambda a}{8\varepsilon_0}$

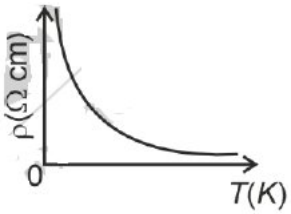
36. Given below are two statements :

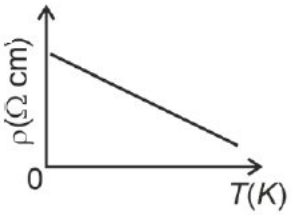
Statement-I : The equivalent emf of two nonideal batteries connected in parallel is smaller than either of the two emfs.
Statement-II : The equivalent internal resistance of two nonideal batteries connected in parallel is smaller than the internal resistance of either of the two batteries.

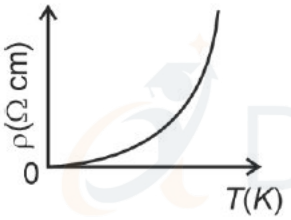
In the light of the above statements, choose the correct answer from the options given below.
(1) Statement-I is false but Statement-II is true
(2) Statement-I is true but Statement-II is false
(3) Both Statement-I and Statement-II are true
(4) Both Statement-I and Statement-II are false

37. Which of the following resistivity (ρ) v/s temperature (T) curves is most suitable to be used in wire bound standard resistors?

(1) 

(2) 

(3) 

(4) 

38. A closed organ and an open organ tube are filled by two different gases having same bulk modulus but different densities ρ_1 and ρ_2, respectively. The frequency of 9^{th} harmonic of closed tube is identical with 4^{th} harmonic of open tube. If the length of the closed tube is 10 cm and the density ratio of the gases is $\rho_1:\rho_2 = 1:16$, then the length of the open tube is :

(1) $\frac{15}{7}$ cm

(2) $\frac{20}{9}$ cm

(3) $\frac{15}{9}$ cm

(4) $\frac{20}{7}$ cm

39. Given is a thin convex lens of glass (refractive index μ) and each side having radius of curvature R. One side is polished for complete reflection. At what distance from the lens, an object be placed on the optic axis so that the image gets formed on the object itself?

(1) R/μ

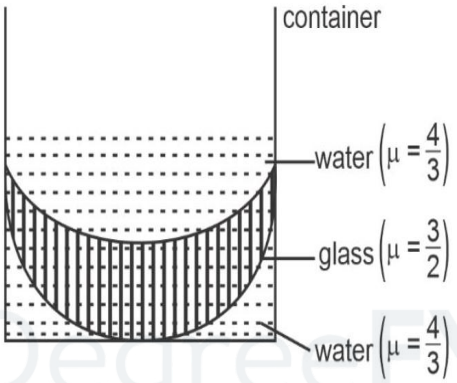
(2) μR

(3) $R/(2\mu - 1)$

(4) $R/(2\mu - 3)$

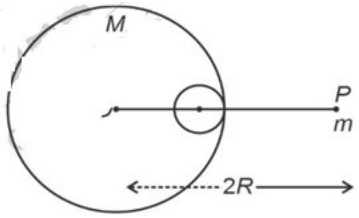
40. Two spherical bodies of same materials having radii 0.2 m and 0.8 m are placed in same atmosphere. The temperature of the smaller body is 800 K and temperature of the bigger body is 400 K . If the energy radiated from the smaller body is E, the energy radiated from the bigger body is (assume, effect of the surrounding temperature to be negligible),
(1) E
(2) $64E$
(3) $256E$
(4) $16E$

41. In the diagram given below, there are three lenses formed. Considering negligible thickness of each of them as compared to $|R_1|$ and $|R_2|$, i.e., the radii of curvature for upper and lower surface of the glass lens, the power of the combination is



(1) $\frac{1}{6}\left(\frac{1}{|R_1|} - \frac{1}{|R_2|}\right)$
(2) $-\frac{1}{6}\left(\frac{1}{|R_1|} - \frac{1}{|R_2|}\right)$
(3) $-\frac{1}{6}\left(\frac{1}{|R_1|} + \frac{1}{|R_2|}\right)$
(4) $\frac{1}{6}\left(\frac{1}{|R_1|} + \frac{1}{|R_2|}\right)$

42. A small point of mass m is placed at a distance $2R$ from the centre ' O ' of a big uniform solid sphere of mass M and radius R. The gravitational force on ' m ' due to M is F_1. A spherical part of radius $\frac{R}{3}$ is removed from the big sphere as shown in the figure and the gravitational force on m due to remaining part of M is found to be F_2. The value of ratio $F_1:F_2$ is



(1) 12:9
(2) 11:10
(3) 12:11
(4) 16:9

43. Given below are two statements :

Statement-I: In a vernier callipers, one vernier scale division is always smaller than one main scale division.

Statement-II: The vernier constant is given by one main scale division multiplied by the number of vernier scale divisions.

In the light of the above statements, choose the correct answer from the options given below.
(1) Both Statement-I and Statement-II are true
(2) Both Statement-I and Statement-II are false
(3) Statement-I is false but Statement-II is true
(4) Statement-I is true but Statement-II is false

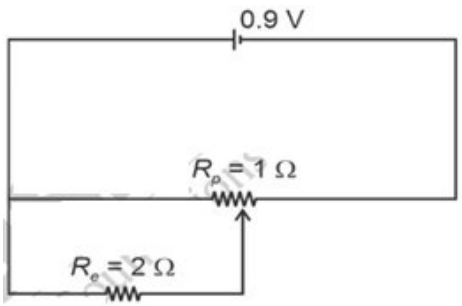
44. Given below are two statements: one is labelled as Assertion (A) and the other is labelled as Reason (R).

Assertion-(A): If Young's double slit experiment is performed in an optically denser medium than air, then the consecutive fringes come closer.

Reason-(R): The speed of light reduces in an optically denser medium than air while its frequency does not change.

In the light of the above statements, choose the most appropriate answer from the options given below:
(1) Both (A) and (R) are true and (R) is the correct explanation of (A)
(2) (A) is true but (R) is false
(3) Both (A) and (R) are true but (R) is not the correct explanation of (A)
(4) (A) is false but (R) is true

45.



Sliding contact of a potentiometer is in the middle of the potentiometer wire having resistance $R_p = 1\Omega$ as shown in the figure. An external resistance of $R_e = 2\Omega$ as connected via the sliding contact. The electric current in the circuit is :
(1) 1.35 A
(2) 1.0 A
(3) 0.3 A
(4) 0.9 A

SECTION - B

Numerical Value Type Questions: This section contains 5Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

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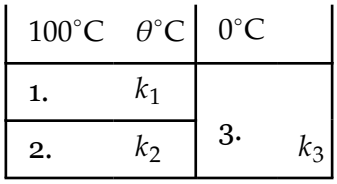
46. The position vectors of two 1 kg particles, (A) and (B), are given by $\vec{r}_A = \left(\alpha_1 t^2 \hat{i} + \alpha_2 t \hat{j} + \alpha_3 t \hat{k}\right)$ m and $\vec{r}_B = \left(\beta_1 t \hat{i} + \beta_2 t^2 \hat{j} + \beta_3 t \hat{k}\right)$ m, respectively; ($\alpha_1 = 1$ m/s^2,$\alpha_2 = 3n$ m/s^2,$\alpha_3 = 2$ m/s,$\beta_1 = 2$ m/s, $\beta_2 = -1$ m/s^2,$\beta_3 = 4p$ m/s), where t is time, n and p are constants. At $t = 1$ s, $\left|\vec{V}_A\right| = \left|\vec{V}_B\right|$ and velocities $\vec{V}_A$ and $\vec{V}_B$ of the particles are orthogonal to each other. At $t = 1$ s, the magnitude of angular momentum of particle (A) with respect to the position of particle (B) is $\sqrt{L}$kgm^2 s^{-1}. The value of L is ____ .

47. The driver sitting inside a parked car is watching vehicles approaching from behind with the help of his side view mirror, which is a convex mirror with radius of curvature $R = 2$ m. Another car approaches him from behind with a uniform speed of 90 km/hr. When the car is at a distance of 24 m from him, the magnitude of the acceleration of the image of the car in the side view mirror is ' a '. The value of 100 a is ____ m/s^2.

48. A particle is projected at an angle of 30° from horizontal at a speed of 60 m/s. The height traversed by the particle in the first second is h_0 and height traversed in the last second, before it reaches the maximum height, is h_1. The ratio h_0:h_1 is ____ . [Take, $g = 10$ m/s^2]

49. Two soap bubbles of radius 2 cm and 4 cm , respectively, are in contact with each other. The radius of curvature of the common surface, in cm, is ____ .

50. Three conductors of same length having thermal conductivity k_1,k_2 and k_3 are connected as shown in figure.



Area of cross sections of 1st and 2nd conductor are same and for 3rd conductor it is double of the 1st conductor. The temperature are given in the figure. In steady state condition, the value of θ is ____ °C.
(Given : $k_1 = 60 Js^{-1} m^{-1} K^{-1}$,$k_2 = 120 Js^{-1} m^{-1} K^{-1}$, $k_3 = 135 Js^{-1} m^{-1} K^{-1}$)

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer :

51. How many different stereoisomers are possible for the given molecule?



(1) 2
(2) 4
(3) 3
(4) 1

52. Given below are two statements:

Statement I : $CH_3 - O - CH_2 - Cl$ will undergo S_N1 reaction though it is a primary halide.

Statement II :

Cl

will not undergo S_N2 reaction very easily though it is a primary halide.
In the light of the above statements, choose the most appropriate answer from the options given below:
(1) Both Statement I and Statement II are incorrect
(2) Both Statement I and Statement II are correct
(3) Statement I is correct but Statement II is incorrect
(4) Statement I is incorrect but Statement II is correct

53. A liquid when kept inside a thermally insulated closed vessel at 25°C was mechanically stirred from outside. What will be the correct option for the following thermodynamic parameters?
(1) $\Delta U > 0, q = 0, w > 0$
(2) $\Delta U < 0, q = 0, w > 0$
(3) $\Delta U = 0, q < 0, w > 0$
(4) $\Delta U = 0, q = 0, w = 0$

54. In which of the following complexes the CFSE, Δ_0 will be equal to zero?
(1) $K_3[Fe(SCN)_6]$
(2) $\left[Fe(en)_3\right]Cl_3$
(3) $[Fe(NH_3)_6]Br_2$
(4) $K_4[Fe(CN)_6]$

55. Which of the following electronegativity order is incorrect?
(1) Mg < Be < B < N
(2) AI < Si < C < N
(3) Al < Mg < B < N
(4) S < Cl < O < F

56. The incorrect statements regarding geometrical isomerism are
(A) Propene shows geometrical isomerism.
(B) Trans isomer has identical atoms/groups on the opposite sides of the double bond.
(C) Cis-but-2-ene has higher dipole moment than trans-but-2-ene.
(D) 2-methylbut-2-ene shows two geometrical isomers.
(E) Trans-isomer has lower melting point than cis isomer.

Choose the correct answer from the options given below.
(1) (A), (D) and (E) only
(2) (A) and (E) only
(3) (C),

(D) and (E) only
(4) (B) and (C) only

57. From the magnetic behaviour of $[NiCl_4]^{2-}$ (paramagnetic) and $[Ni(CO)_4]$ (diamagnetic), choose the correct geometry and oxidation state.
(1) $[NiCl_4]^{2-}$:Ni^{il}, square planar
$[Ni(CO)_4]$:Ni(0), square planar
(2) $[NiCl_4]^{2-}$:Ni^{II}, tetrahedral
$[Ni(CO)_4]$:Ni(0), tetrahedral
(3) $[NiCl_4]^{2-}$:Ni(0), tetrahedral
$[Ni(CO)_4]$:Ni(0), square planar
(4) $[NiCl_4]^{2-}$:Ni^{II}, tetrahedral
$[Ni(CO)_4]$: Nill, square planar

58. Given below are two statements :

Statement 1 : One mole of propyne reacts with excess of sodium to liberate half a mole of H_2 gas.

Statement II : Four g of propyne reacts with $NaNH_2$ to liberate NH_3 gas which occupies 224 mL at STP.

In the light of the above statements, choose the most appropriate answer from the options given below.
(1) Both Statement I and Statement II are correct
(2) Statement I is incorrect but Statement II is correct
(3) Statement I is correct but Statement II is incorrect
(4) Both Statement I and Statement II are incorrect

59. Lanthanoid ions with $4f^7$ configuration are
(A) Eu^{2+}
(B) Gd^{3+}
(C) Eu^{3+}
(D) Tb^{3+}
(E) Sm^{2+}

Choose the correct answer from the options given below.

(1) (A) and (B) only
(2) (A) and (D) only
(3) (B) and (E) only

(4) (B) and (C) only

List-I

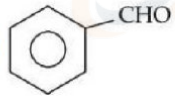
(A) $Al^{3+} < Mg^{2+} < Na^{+} < F^{-}$
(B) B < C < O < N
(C) B < Al < Mg < K
(D) Si < P < S < Cl

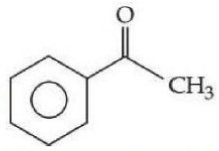
60. Match List-I with List-II.

List-I	List-II
(A) Al3+ < Mg2+ < Na+ < F-	(I) Ionisation enthalpy
(B) B < C < O < N	(II) Metallic character
(C) B < Al < Mg < K	(III) Electronegativity
(D) Si < P < S < Cl	(IV) Ionic radii

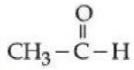
Choose the correct answer from the options given below.
(1) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)
(2) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)
(3) (A)-(II), (B)-(III), (C)-(IV), (D)-(I)
(4) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)

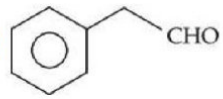
61. The compounds which give positive Fehling's test are:

(A) 

(B) 

(C) $HOCH_2 - CO - (CHOH)_3 - CH_2 - OH$

(D) 

(E) 

Choose the correct answer from the options given below:
(1) (C), (D) and (E) Only
(2) (A), (B) and (C) Only
(3) (A), (D) and (E) Only
(4) (A), (C) and (D) Only

62. The IUPAC name of the following compound is:



(1) Methyl-5-carboxy-2-methylhexanoate.
(2) 6-Methoxycarbonyl-2,5-dimethylhexanoic acid.
(3) Methyl-6-carboxy-2,5-dimethylhexanoate.
(4) 2-Carboxy-5-methoxycarbonylhexane.

63. A solution of aluminium chloride is electrolysed for 30 minutes using a current of 2 A . The amount of the aluminium deposited at the cathode is ____ .
[Given: molar mass of aluminium and chlorine are 27 g mol^{-1} and 35.5 g mol^{-1} respectively. Faraday constant = 96500Cmol^{-1}]
(1) 0.336 g
(2) 0.441 g
(3) 1.007 g
(4) 1.660 g

64. Which of the following statement is not true for radioactive decay?
(1) Half life is ln 2 times of $\frac{1}{\text{rate constant}}$.
(2) Decay constant increases with increase in temperature.
(3) Amount of radioactive substance remained after three half lives is $\frac{1}{8}$ th of original amount.
(4) Decay constant does not depend upon temperature.

65. Radius of the first excited state of Helium ion is given as:
a_0 → radius of first stationary state of hydrogen atom.
(1) $r = \frac{a_0}{2}$
(2) $r = \frac{a_0}{4}$
(3) $r = 2a_0$
(4) $r = 4ao$

66. The IUPAC name of the following compound is:



(1) Methyl-5-carboxy-2-methylhexanoate.
(2) 6-Methoxycarbonyl-2,5-dimethylhexanoic acid.

(3) Methyl-6-carboxy-2,5-dimethylhexanoate.
(4) 2-Carboxy-5-methoxycarbonylhexane.

67. Which of the following electrolyte can be used to obtain $H_2S_2O_8$ by the process of electrolysis?
(1) Dilute solution of sulphuric acid
(2) Dilute solution of sodium sulphate
(3) Acidified dilute solution of sodium sulphate
(4) Concentrated solution of sulphuric acid

68. Arrange the following solutions in order of their increasing boiling points.
(i) 10^{-4}MNaCl
(ii) 10^{-4}M Urea
(iii) 10^{-3}MNaCl
(iv) 10^{-2}MNaCl
(1) (ii) < (i) ≡ (iii) < (iv)
(2) (i) < (ii) < (iii) < (iv)
(3) (iv) < (iii) < (i) < (ii)
(4) (ii) < (i) < (iii) < (iv)

69. A vessel at 1000 K contains CO_2 with a pressure of 0.5 atm . Some of CO_2 is converted into CO on addition of graphite. If total pressure at equilibrium is 0.8 atm , then Kp is:
(1) 0.18 atm
(2) 1.8 atm
(3) 0.3 atm
(4) 3 atm

70. Which of the following acids is a vitamin?
(1) Saccharic acid
(2) Adipic acid
(3) Aspartic acid
(4) Ascorbic acid

SECTION - B

Numerical Value Type Questions: This section contains 5Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

71. In Carius method for estimation of halogens, 180 mg of an organic compound produced 143.5 mg of AgCl . The percentage composition of chlorine in the compound is ____ %.
(Given : molar mass in $gmol^{-1}$ of Ag:108,Cl:35.5)

72. Some CO_2 gas was kept in a sealed container at a pressure of 1 atm and at 273 K . This entire amount of CO_2 gas was later passed through an aqueous solution of $Ca(OH)_2$. The excess unreacted $Ca(OH)_2$ was later neutralized with 0.1 M of 40 mL HCl . If the volume of the sealed container of CO_2 was x , then x is ____ cm^3 (nearest integer).

[Given : The entire amount of CO_2(g) reacted with exactly half the initial amount of $Ca(OH)_2$ present in the aqueous solution]

73. The number of molecules/ions that show linear geometry among the following is ____.

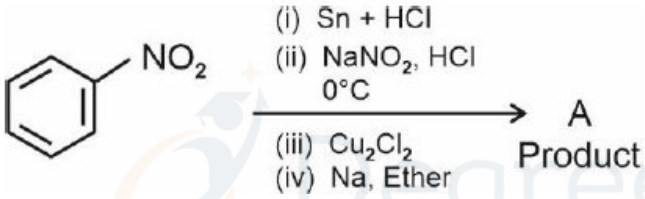
SO_2,$BeCl_2$,CO_2, N_3^-,NO_2, F_2O,XeF_2,NO_2^+,I_3^-,O_3

74.

$$A \rightarrow B$$

The molecule A changes into its isomeric form B by following a first order kinetics at a temperature of 1000 K . If the energy barrier with respect to reactant energy for such isomeric transformation is 191.48 $kJmol^{-1}$ and the frequency factor is 10^{20}, the time required for 50% molecules of *A* to become *B* is ____ picoseconds (nearest integer). [R = 8.314 $J\ K^{-1}\ mol^{-1}$]

75. Consider the following sequence of reactions :



Molar mass of the product formed (A) is _____ $g\ mol^{-1}$.

Answers and Solutions JEE (Main)-2025 Phase-1

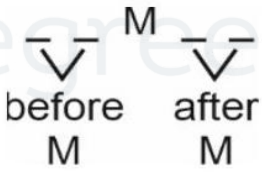
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MATHEMATICS

SECTION A

1.

Answer (4)
Sol.



M is at 13^{th} position
$\Rightarrow \left[{}^{12}C_2 \cdot (1)\right]_{\text{before M,}} [1]_{\text{M,}} \left[{}^{13}C_2(1)\right]_{\text{after M}}$ ways
$= 5148$

2. Answer (4)
Sol. Let $f(x) = 16\left[\left(\sec^{-1} x\right)^2 + \left(\text{cosec}^{-1}x\right)^2\right]$

$$f(x) = 16\left[\left(\sec^{-1} x + \text{cosec}^{-1}x\right)^2 - 2\left(\sec^{-1} x\right)\left(\frac{\pi}{2} - \sec^{-1} x\right)\right]$$
$$= 16\left[\frac{\pi^2}{4} - \pi\sec^{-1} x + 2\sec^{-1} x\right], \sec^{-1} x \in [0,\pi] - \left\{\frac{\pi}{2}\right\}$$
$$= 16\left[2\left(\sec^{-1} x - \frac{\pi}{4}\right)^2 + \frac{\pi^2}{4} - \frac{\pi^2}{8}\right]$$

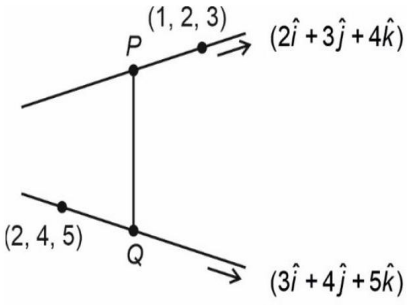
$f(x)$ minimum at $\sec^{-1} x = \frac{\pi}{4}$ and maximum at $\sec^{-1} x = \pi$
$\Rightarrow f(x)_{\min} = 2\pi^2, f(x)_{\max} = 20\pi^2$

3. Answer (1)
Sol. Number of non-empty equivalence relations on the set {1,2,3} will be bell number $3 = 5$
{{1},{2},{3}},
{{1,2},{3}},{{1,3},{2},{2,3},{1}},
{{1,2,3}}. Therefore, total non-empty equivalence relation is 5 .

4. Answer (3)

Sol. $L_1: \frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$

$$L_2: \frac{x-2}{3} = \frac{y-4}{4} = \frac{z-5}{5}$$



$P(2\lambda+1, 3\lambda+2, 4\lambda+3)$
$Q(3\mu+2, 4\mu+4, 5\mu+5)$
Dr's of $PQ < 2\lambda-3\mu-1, 3\lambda-4\mu-2,$
$4\lambda-5\mu-2 >$

$$PQ = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{vmatrix} = -\hat{i} + 2\hat{j} - \hat{k}$$

$$\Rightarrow \frac{2\lambda-3\mu-1}{-1} = \frac{3\lambda-4\mu-2}{2} = \frac{4\lambda-5\mu-2}{-1}$$

$$\Rightarrow \lambda = \frac{1}{3} \mu = \frac{-1}{6}$$

$$\Rightarrow P\left(\frac{5}{3}, 3, \frac{13}{3}\right) Q\left(\frac{3}{2}, \frac{10}{3}, \frac{25}{6}\right)$$

Dr's $PQ\langle 1, -2, 1\rangle$
$\therefore$ Line

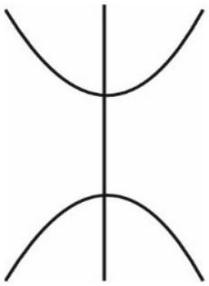
$$\frac{y-\frac{5}{3}}{1} = \frac{y-3}{-2} = \frac{y-\frac{13}{3}}{1}$$

$\therefore$ Option (3) satisfies

5. Answer (2)

Sol. $\left|SP - S'P\right| = 2a$
$SS' = 2ae$
S(1,14) S′(1, − 12) P(1,6)
$2a = |8 - 18|$
$a = 5$

$2ae = 26 \Rightarrow ae = 13$



$$L(LR) = \frac{2b^2}{a} = \frac{2a^2\left(e^2-1\right)}{a}$$
$$= \frac{2[169-25]}{5} = \frac{288}{5}$$

6. Answer (1)
Sol.

	x_i	P_i
HHH	0	$\frac{1}{8}$
TTT	0	$\frac{1}{8}$
HHT	1	$\frac{1}{8}$
HTH	1	$\frac{1}{8}$
THH	0	$\frac{1}{8}$
TTH	0	$\frac{1}{8}$
THT	1	$\frac{1}{8}$
HTT	1	$\frac{1}{8}$

$$\mu = \sum x_i P_i = \frac{1}{2}$$
$$\sigma^2 = \sum x_i^2 P_i - \mu^2$$

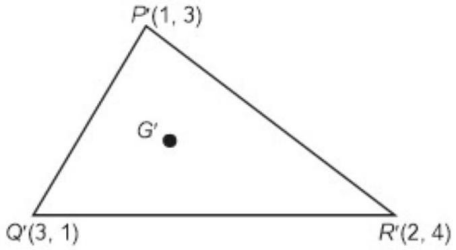
$= \frac{1}{2} - \frac{1}{4} = \frac{1}{4}$

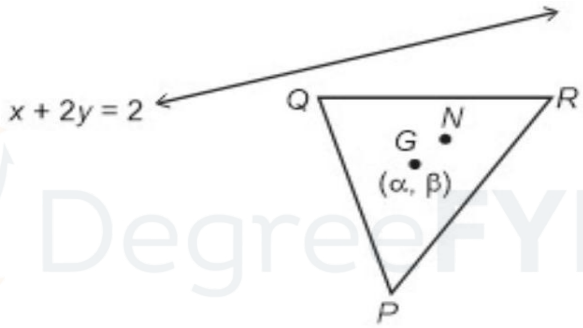
$64\left(\mu + \sigma^2\right) = 64\left[\frac{1}{2} + \frac{1}{4}\right]$

$= 64 \times \frac{3}{4} = 48$

7. Answer (3)

Sol. The centroid $G''(\alpha,\beta)$ of $\triangle PQR$ be image of centroid of given triangle $P'Q'R'$.





Centroid of $\Delta P'Q'R' = \left(\frac{1+3+2}{3}, \frac{3+1+4}{3}\right) = G'\left(2, \frac{8}{3}\right)$.

Image of $G'\left(2, \frac{8}{3}\right)$, w.r.t. line $x + 2y = 2$ is (α,β)

Then $\frac{\alpha-2}{1} = \frac{\beta-\frac{8}{3}}{2} = \frac{-2\left(2+\frac{16}{3}-2\right)}{1+4}$

$\therefore \quad \frac{\alpha-2}{1} = \frac{\beta-\frac{8}{3}}{2} = -\frac{32}{15}$

$\therefore \ \alpha = -\frac{2}{15}$ and $\beta = -\frac{8}{5}$

Then $15(\alpha-\beta) = 15\left(-\frac{2}{15} + \frac{24}{15}\right) = 22$

8. Answer (3)

Sol. $\because f(x+y) = f(x).f'(y) + f'(x).f(y), \forall x,y \in R$

And $f(0) = 1$

Now replace x by zero and y by zero we get

$f(0) = f(0)f'(0) + f'(0)f(0)$

$1 = f'(0) + f'(0)$

$$f'(0) = \frac{1}{2} \#(iii)$$

Now replace y by zero in equation (i), we get

$f(x) = \frac{1}{2}f(x) + f'(x)$

or, $\frac{1}{2}f(x) = f'(x)$

then $\frac{f'(x)}{f(x)} = \frac{1}{2}$

hence $\ln |f(x)| = \frac{x}{2} + c$

Put $x = 0$, we get $c = 0$

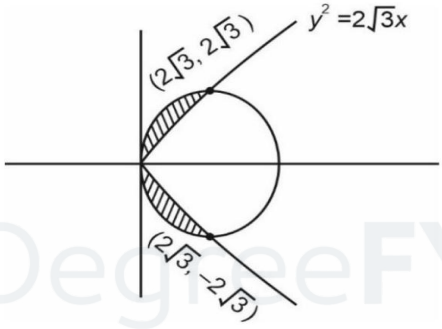
$\therefore \ln |f(x)| = \frac{x}{2}$

Then $\sum_{n=1}^{100} \ln (f(\eta)) = \left(\frac{1}{2} + \frac{2}{2} + \frac{3}{2} + \ldots + \frac{100}{2}\right)$

$= \frac{5050}{2} = 2525$

9. Answer (3)

Sol.



Required area $= 2\int_0^{2\sqrt{3}} \left(\sqrt{4\sqrt{3}x - x^2} - \sqrt{2\sqrt{3}x}\right) dx$

$= 2\int_0^{2\sqrt{3}} \left(\sqrt{12 - (x - 2\sqrt{3})^2} - \sqrt{2\sqrt{3}x}\right) dx$

$= 2\left[\frac{x - 2\sqrt{3}}{2}\sqrt{12 - (x - 2\sqrt{3})^2} + \frac{12}{2}\sin^{-1}\left(\frac{x - 2\sqrt{3}}{2\sqrt{3}}\right) - \frac{\sqrt{2\sqrt{3}}x^{\frac{3}{2}}}{\frac{3}{2}}\right]_0^{2\sqrt{3}}$

$= 2\{3\pi - 8\}$

$= 6\pi - 16$ sq. units.

10. Answer (4)

Sol. $a_1 a_5 = 28 \Rightarrow a^2 r^4 = 28$

$a_2 + a_4 = 29 \Rightarrow ar + ar^3 = 29$

ar and ar^3 are roots of

$k^2 - 29k + 28 = 0$

$\Rightarrow k = 1, k = 28$

$ar = 1, ar^3 = 28$

$r^2 = 28, a^2 = \frac{1}{28}$

$a_6 = ar^5 \Rightarrow a_6^2 = a^2 r^{10} = (28)^4$

$\Rightarrow a_6 = 784$

11. Answer (2)
Sol. $|z| = 1$

$$\arg\ (z_1) = -\frac{\pi}{4}, \arg\ (z_2) = 0, \arg\ (z_3) = \frac{\pi}{4}$$

$$z_1 = |1|e^{-\frac{\pi}{4}} = \frac{1}{\sqrt{2}} - \frac{i}{\sqrt{2}}$$

$$z_2 = 1 + 0i$$

$$z_3 = \frac{1}{\sqrt{2}} + \frac{i}{\sqrt{2}}$$

$$\overline{z_1 z_2} = \frac{1-i}{\sqrt{2}}$$

$$\overline{z_2 z_3} = \frac{1-i}{\sqrt{2}}$$

$$\overline{z_3 z_1} = \frac{(1+i)^2}{2}$$

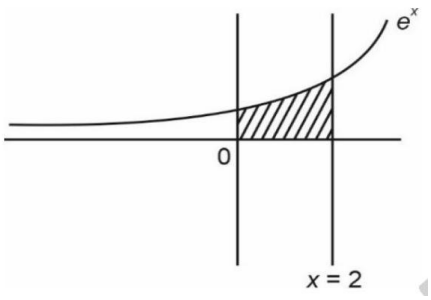
$$\overline{z_1 z_2} + \overline{z_2 z_3} + \overline{z_3 z_1} = \sqrt{2} + i(1-\sqrt{2})$$

$$\left|\overline{z_1 z_2} + \overline{z_2 z_3} + \overline{z_3 z_1}\right|^2 = 5 - 2\sqrt{2}$$

$\alpha = 5, \beta = -2$

$\alpha^2 + \beta^2 = 29$

12. Answer (1)
Sol. $f(x+y) = f(x)f(y)$
$\Rightarrow$ Take $f(x) = k^x$
$k^x \log\ (k) = f'(x)$
$\log\ k = 4a \Rightarrow k = e^{4a}$
$f(x) = e^{4ax}$
$f''(x) - 3af'(x) - f(x) = 0$
$16a^2e^{4ax} - 12a^2e^{4ax} - e^{4ax} = 0$
$\Rightarrow a^2 = \frac{1}{4} \Rightarrow a = \frac{1}{2}$
$f(x) = e^{2x}$



$\int_0^2 (e^x)\,dx = e^2 - 1$

13. Answer (2)

Sol. $y^2dx + \left(x - \frac{1}{y}\right)dy = 0$

$y^2dx = \left(\frac{1}{y} - x\right)dy$

$\Rightarrow y^2\frac{dx}{dy} = \frac{1}{y} - x$

$\Rightarrow \frac{dx}{dy} + \frac{x}{y^2} = \frac{1}{y^3}$

I.F. $= e^{\int \frac{1}{y^2}dy} = e^{\frac{-1}{y}}$

$\therefore$ Solution is

$xe^{\frac{-1}{y}} = \int e^{-\frac{1}{y}} \times \frac{1}{y^3}dy + C$

Let $\frac{-1}{y} = t$

$\Rightarrow \frac{1}{y^2}dy = dt$

$\Rightarrow xe^{-\frac{1}{y}} = -\int e^t t\,dt + C$

$\Rightarrow xe^{-\frac{1}{y}} = -e^t(t-1) + C$

$\Rightarrow xe^{-\frac{1}{y}} = -e^{\frac{-1}{y}}\left(\frac{-1}{y} - 1\right) + C$

$x(1) = 1$

$\Rightarrow e^{-1} = -e^{-1}(-2) + C$

$\Rightarrow C = -e^{-1}$

$\Rightarrow x = \frac{1}{y} + 1 - e^{-1+\frac{1}{y}}$

$x\left(\frac{1}{2}\right) = 3 - e$

14. Answer (3)

Sol. Bag contains 4 white and 6 black balls

A : first ball selected is black

B : Second ball is also black

$P\left(\frac{A}{B}\right) = \frac{\frac{6}{10}\times\frac{5}{9}}{\frac{4}{10}\times\frac{6}{9} + \frac{6}{10}\times\frac{5}{9}} = \frac{30}{24+30}$

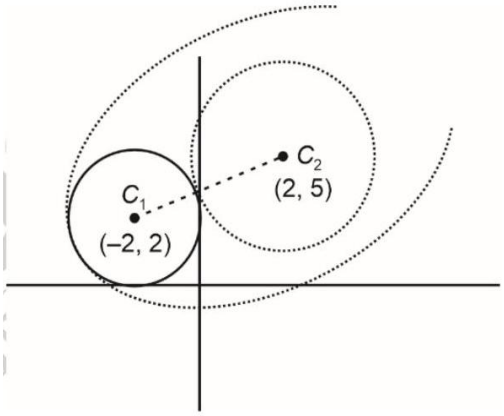
$= \frac{30}{54} = \frac{5}{9}$
$m + n = 5 + 9 = 14$

15. Answer (4)
Sol. $y = x^2 + px - 3$ is a parabola
at $x = 0 \Rightarrow y = -3$
Parabola cuts the y-axis at $(0, -3)$
Equation of circle will be
$(x+1)^2 + (y+1)^2 = (0+1)^2 + (-3+1)^2$
$\Rightarrow (x+1)^2 + (y+1)^2 = 5$
$\Rightarrow x^2 + y^2 + 2x + 2y - 3 = 0$
Now this circle cuts x-axis at $y = 0$
$x^2 + 2x - 3 = 0$
$\Rightarrow (x+3)(x-1) = 0$
$\Rightarrow x = -3, 1$
$(-3, 0)$ and $(1, 0)$

Points P, Q and R are $(0, -3)(-3, 0)$ and $(1, 0)$
Area of $(\triangle PQR) = \frac{1}{2}\begin{vmatrix} 0 & -3 & 1 \\ -3 & 0 & 1 \\ 1 & 0 & 1 \end{vmatrix}$
$= \frac{1}{2} \times 12 = 6$
$\Rightarrow$ Option (4) is correct.

16. Answer (3)

Sol.



$C_1C_2 = \sqrt{(2+2)^2 + (5-2)^2}$
$= \sqrt{16+9}$
$= 5$
$r + 2 > 5$
$r > 3$
$r < 5 + 2$
$r < 7$
$\therefore \alpha = 3, \beta = 7$
$3\beta - 2\alpha = 3(7) - 2(3) = 21 - 6 = 15$

17. Answer (4)

Sol. $T_n = S_n - S_{n-1}$

$$= \frac{(2n-1)(2n+1)(2n+3)(2n+5) -}{(2n-3)(2n-1)(2n+1)(2n+3)}$$

$$T_n = \frac{(2n-1)(2n+1)(2n+3)}{8}$$

$$\frac{1}{T_n} = 2\left(\frac{1}{(2n-1)(2n+1)} - \frac{1}{(2n-1)(2n+3)}\right)$$

$$S_n = 2\left(\frac{1}{1\times 3} - \frac{1}{(2n-1)(2n+3)}\right)$$

$$\lim_{n\to\infty} S_n = \frac{2}{3}$$

18. Answer (2)

Sol. Number of elements in set B, corresponding to
$m = 1$ are 9
$m = 2$ are $n = 3,5,7,9 = 4$
$m = 3$ are $n = 4,5,7,8,10 = 5$
$m = 4$ are $n = 5,7,9 = 3$
$m = 5$ are $n = 6,7,8,9 = 4$
$m = 6$ are $n = 7 = 1$
$m = 7$ are $n = 8,9,10 = 3$
$m = 8$ are $n = 9 = 1$
$m = 9$ are $n = 10 = 1$
Total number $= 9 + 4 + 5 + 3 + 4 + 1 + 3 + 1 + 1$
$= 31$

19. Answer (3)

Sol. $e^{5(\log_e x)^2+3} = e^{\log x^8}$

$\Rightarrow 5(\log_e x)^2 + 3 = \log x^8 = 8\log_e x$

Put $\log_e x = t, 5t(t-1) - 3(t-1) = 0$

$$\Rightarrow 5t^2 - 8t + 3 = 0$$
$$\Rightarrow 5t^2 - 5t - 3t + 3 = 0$$
$$(5t-3)(t-1) = 0$$
$$t = 1 \Rightarrow \log_e x = 1 \Rightarrow x = e$$
$$t = \frac{3}{5} \Rightarrow \log_e x = \frac{3}{5} \Rightarrow x = e^{\frac{3}{5}}$$

Product of all roots $= e^{1+\frac{3}{5}} = e^{\frac{8}{5}}$
Option = 3

20. Answer (3)

Sol. $f(x) = 7\tan^8 x + 7\tan^6 x - 3\tan^4 x - 3\tan^2 x$

$$= 7\tan^6 x\left(1+\tan^2 x\right) - 3\tan^2 x\left(1+\tan^2 x\right)$$
$$= \left(7\tan^6 x - 3\tan^2 x\right)\left(1+\tan^2 x\right)$$
$$= \left(7\tan^6 x - 3\tan^2 x\right)\sec^2 x$$
$$I_1 = \int_0^{\frac{\pi}{4}} f(x)dx = \int_0^{\frac{\pi}{4}} \left(7\tan^6 x - 3\tan^2 x\right)\sec^2 x dx$$
$$= \left(\frac{7\tan^7 x}{7} - \frac{3\tan^3 x}{3}\right)\Big|_0^{\frac{\pi}{4}} = 1 - 1 = 0$$

$$I_2 = \int_0^{\frac{\pi}{4}} xf(x)dx = \int_0^{\frac{\pi}{4}} x\left(7\tan^6 x - 3\tan^2 x\right)\sec^2 x dx$$
$$= x\left(\tan^7 x - \tan^3 x\right)\Big|_0^{\frac{\pi}{4}} - \int_0^{\frac{\pi}{4}} 1\cdot\left(\tan^7 x - \tan^3 x\right)dx$$
$$= 0 - \int_0^{\frac{\pi}{4}} \tan^3 x\left(\tan^2 x - 1\right)\left(\tan^2 x + 1\right)dx$$
$$= \int_0^{\frac{\pi}{4}} \left(\tan^3 x - \tan^5 x\right)\sec^2 x dx = \frac{\tan^4 x}{4} - \frac{\tan^6 x}{6}\Big|_0^{\frac{\pi}{4}}$$
$$= \frac{1}{12}$$

Hence $7/_1 + 12/_2 = 1$

SECTION - B

Numerical Value Type Questions: This section contains 5 Numerical based questions. The answer to each question should be rounded-off to the nearest integer..

21. Answer (16)

Sol. $\vec{c} = \left(\frac{\vec{b}\cdot\vec{a}}{|\vec{b}|}\right)\frac{\vec{a}}{|\vec{a}|}$

$$\left(\frac{\lambda+8}{9}\right)(\hat{i}+2\hat{j}+2\hat{k})$$
$$|\vec{a}+\vec{c}| = 7$$
$$\Rightarrow \left|\left(\frac{\lambda+8}{9}+1\right)\hat{i} + \left(\frac{2(\lambda+8)}{9}+2\right)\hat{j} + \left(\frac{2(\lambda+8)}{9}+2\right)\hat{k}\right| = 7$$
$$\left(\frac{\lambda+8}{9}+1\right)^2 + \left(\frac{2(\lambda+8)}{9}+2\right)^2 + \left(\frac{2(\lambda+8)}{9}+2\right)^2 = 49$$
$$\Rightarrow \lambda = 4 \Rightarrow \vec{c} = \frac{4}{3}\hat{i} + \frac{8}{3}\hat{j} + \frac{8}{3}\hat{k}$$
$$\text{Area of parallelogram} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{4}{3} & \frac{8}{3} & \frac{8}{3} \\ 4 & 0 & 4 \end{vmatrix} = 16$$

22. Answer (2035)

Sol. $(1+x)^{11} = {}^{11}C_0 + {}^{11}C_1x + {}^{11}C_2x^2 + \cdots + {}^{11}C_{11}x^{11}$

$$\int_0^1 (1+x)^{11}dx = \int_0^1 \left({}^{11}C_0 + {}^{11}C_1x + {}^{11}C_2x^2 + \cdots + {}^{11}C_{11}x^{11}\right)dx$$

$$\frac{(1-x)^{12}}{12}\Big]_0^1 = {}^{11}C_{0x} + \frac{{}^{11}C_1x}{2} + \frac{{}^{11}C_2x}{3} + \cdots + \frac{{}^{11}C_{11}x^{12}}{12}\Big]_0^1$$

$$\frac{2^{12}-1}{12} = C_0 + \frac{C_1}{2} + \frac{C_2}{3} + \cdots + \frac{C_{11}}{12} \ldots (1)\ (1)$$

Now,

$$\int_{-1}^0 (1+x)^{11}dx = \int_{-1}^0 \left({}^{11}C_0 + {}^{11}C_1x + {}^{11}C_2x^2 + \cdots + {}^{11}C_{11}x^{11}\right)dx$$

$$\frac{(1+x)^{12}}{12}\Big]_{-1}^0 = {}^{11}C_0x + \frac{{}^{11}C_1x^2}{2} + \frac{{}^{11}C_2x^3}{3} + \cdots + \frac{{}^{11}C_{11}x^{12}}{12}\Big]_{-1}^0$$

$$\frac{1}{12} = C_0 - \frac{C_1}{2} + \frac{C_2}{3} \cdots (2)$$

(1) - (2)

$$= \frac{2^{12}-2}{12} = 2\left[\frac{C_1}{2} + \frac{C_3}{4} + \cdots\right]$$

$$\Rightarrow \sum_{r=0}^{5} \frac{C_{2r+1}}{2r+2} = \frac{2^{11}-1}{12} = \frac{2047}{12} = \frac{m}{n}$$

$$= 2047 - 12 = 2035$$

23. Answer (34)

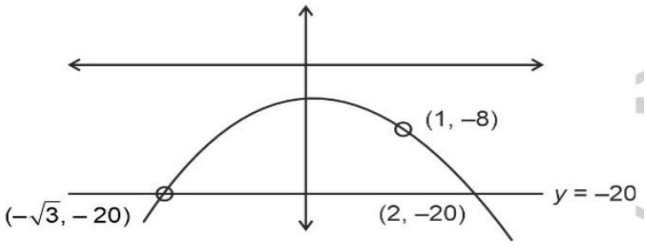
Sol. $f(x)$ is continuous and differentiable

at $x = 1$, LHL = RHL, LHD = RHD

$-3a - 2 = a^2 + b, -6a = b$

$a = 2; b = -12$

$$f(x) = \begin{cases} -6x^2 - 2, & x < 1 \\ 4 - 12x, & x \geq 1 \end{cases}$$



Area $= \int_{-\sqrt{3}}^{1}\left(-6x^2-2+20\right)dx + \int_{1}^{2}(4-12x+20)dx\Big]$

$= 16 + 12\sqrt{3} + 6 = 22 + 12\sqrt{3}$

$\therefore \alpha + \beta = 34$

24. Let $L_1: \frac{x-1}{3} = \frac{y-1}{-1} = \frac{z+1}{0}$ and $L_2: \frac{x-2}{2} = \frac{y}{0} = \frac{z+4}{\alpha}, \alpha \in R$, be two lines, which intersect at the point B. If P is the foot of perpendicular from the point $A(1,1,-1)$ and L_2, then the value of $26\alpha(PB)^2$ is

Answer (216)

Sol. Point B

$(3\lambda + 1, -\lambda + 1, -1) \equiv (2\mu + 2, 0, \alpha\mu - 4)$

$3\lambda + 1 = 2\mu + 2$

$-\lambda + 1 = 0$

$-1 = \alpha\mu - 4$

$\lambda = 1, \mu = 1, \alpha = 3$

$B(4,0,-1)$

Let Point ' P ' is $(2\delta + 2, 0, 3\delta - 4)$

Dr's of AP $< 2\delta + 1, -1, 3\delta - 3 >$

$AP \perp L_2 \Rightarrow \delta = \frac{7}{13}$

$P\left(\frac{40}{13}, 0, \frac{-31}{13}\right)$

$\therefore 26\alpha(PB)^2 = 26 \times 3 \times \left(\frac{144}{169} + \frac{324}{169}\right)$

$= 216$

25. Answer (34)

Sol. As $A\text{adj}A = |A|I, \det(\lambda A) = \lambda^n \det A$

$$\det(3\text{adj}(-6\text{adj}(3A))) = 3^3\det(\text{adj}(-6\text{adj}(3A)))$$
$$= 3^3(-6\text{adj}(3A))^2$$
$$= 3^3(-6)^6|3A|^4$$
$$= 3^9 2^6 \cdot 3^{12} \cdot (-2)^4$$
$$= 3^{21} \cdot 2^{10}$$

Now comparing with given condition

$2^{m+n}3^{mn} = 2^{10} \cdot 3^{21}$

$m + n = 10, mn = 21$

$\Rightarrow m = 7, n = 3 (m > n)$

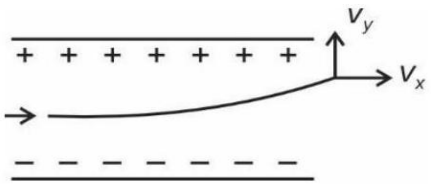
$\therefore 4m + 2n = 28 + 6 = 34$

PHYSICS

SECTION A

26. Answer (2)

Sol.



Horizontal component of velocity will remain same.

$$t = \frac{l}{v_x} = \frac{0.1}{10^6}$$

$$v_y = a_y t = \frac{eE}{m} t$$

$$= \frac{1.6 \times 10^{-19} \times 9.1 \times 10^2}{9.1 \times 10^{-31}} \times \frac{0.1}{10^6}$$

$$= 1.6 \times 10^7$$

27. Answer (2)

Sol. ice at $-10^\circ C \longrightarrow$ ice at $0^\circ C \longrightarrow$ water at $0^\circ C$
vapour at $110^\circ C \longleftarrow$ vapour at $100^\circ C \longleftarrow$ water at 100°

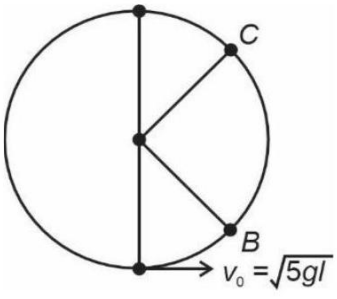
$$Q = 10^{-3}\left[2100 \times 10 + 3.35 \times 10^5 + 100 \times 4180 + 2.25 \times 10^6 + 10 \times 1920\right]$$

28. Answer (2)
Sol. For a current carrying loop at centre

$$B = \frac{\mu_0 i}{2R}$$

$$\therefore \quad \frac{B}{\mu_0} \equiv \frac{i}{R} \equiv \left[AL^{-1}\right]$$

29. Sol.



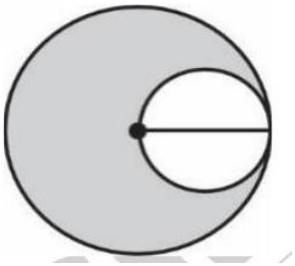
$$v_B = \sqrt{v_0^2 - 2g\left(\frac{l}{2}\right)}$$

$$v_B = \sqrt{4gl}$$

$$v_C = \sqrt{v_0^2 - 3gl} = \sqrt{2gl}$$

$$\frac{K_B}{K_C} = \frac{v_B^2}{v_C^2} = 2$$

30. Answer (3)
Sol.



$$I_{\text{complete}} = \frac{MR^2}{2}$$

$$I_{\text{removed}} = \left(\frac{M}{4}\right)\left(\frac{R}{2}\right)^2\frac{1}{2} + \left(\frac{M}{4}\right)\left(\frac{R}{2}\right)^2$$
$$= \frac{3MR^2}{32}$$
$$I = \frac{MR^2}{2} - \frac{3MMR^2}{32} = \frac{13}{32}MR^2$$

31. Answer (3)

Sol. $C = 40\mu$ F

$$C' = \text{kC} = 80\mu \text{ F}$$
$$V = 100 \text{ V}$$
$$Q = CV = 4\text{mC}$$
$$Q' = C'V = 8\text{mC}$$

$\therefore$ Extra charge = 4mC

$$U_1 = \frac{1}{2}CV^2, U_2 = \frac{1}{2}CV^2$$
$$\Delta U = \frac{1}{2}\left(C' - C\right)V^2$$
$$= \frac{1}{2} \times 40 \times 10^4 \times 10^{-6}$$
$$= 0.2 \text{ J}$$

32. Answer (3)

Sol. E(Energy of incident photon) $= \frac{1240}{550} = 2.25\text{eV}$
$E > \phi_{\text{Cs}}, E < \phi_{\text{Li}}$
$\therefore$ Only cesium will show photoelectric effect.

33. Answer (*)

Sol. According to de-Broglie hypothesis
$2\pi r_n = n\lambda$
$\frac{2\pi r_1}{2\pi r_4} = \frac{\lambda_1}{4\lambda_4}$

$\frac{\lambda_1}{\lambda_4} = 4\left(\frac{r_1}{r_4}\right)$
$r \propto n^2$
$\therefore \ \frac{\lambda_1}{\lambda_4} = \frac{1}{4}$

- None of the option is matching.

34. Answer (4)

Sol. For forward bias potential of p side should be higher than n side.

35. Answer (4)

Sol. Charge of the line charge $= \frac{a\lambda}{2}$
Portion of wire inside cube $= \frac{1}{4}$

$$\therefore \ q_{\text{en}} = \frac{1}{4}\left(\frac{a\lambda}{2}\right) = \frac{a\lambda}{8}$$
$$\phi = \frac{q_{en}}{\varepsilon_0} = \frac{a\lambda}{8\varepsilon_0}$$

36. Answer (1)

Sol. In parallel connections
$\frac{1}{r_{\text{eq}}} = \frac{1}{r_1} + \frac{1}{r_2}$
$\frac{E_{\text{eq}}}{r_{\text{eq}}} = \frac{E_1}{r_1} + \frac{E_2}{r_2}$
If $E_1 = E_2$ and $r_1 = r_2, E_{\text{eq}} = E_1 = E_2$
$\therefore$ Statement I is false.
r_{eq} is less then both r_1 and r_2
$\therefore$ Statement II is true

37. Answer (1)

Sol. For bound standard resistors the resistivity will remain nearly constant.

38. Answer (2)

Sol. $9\left(\frac{v_C}{4I_C}\right) = 4\left(\frac{v_o}{2I_o}\right)$

$$v = \sqrt{\frac{B}{\rho}}$$

$$\therefore \frac{v_c}{v_o} = \sqrt{\frac{\rho_2}{\rho_1}} = 4$$

$$I_O = \frac{8}{9} I_C \left(\frac{v_O}{v_C}\right)$$

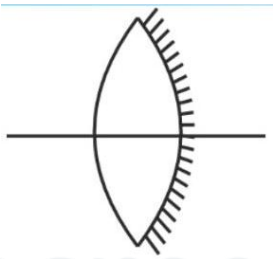
$$= \frac{8}{9} I_C \times \frac{1}{4} = \frac{2}{9} I_C$$

$I_O =$

$\frac{20}{9}$ cm

39. Answer (3)

Sol.



$$-\frac{1}{f_{eq}} = \frac{2}{f_l} - \frac{1}{f_m}$$

$$= 2(\mu - 1)\frac{2}{R} + \frac{2}{R}$$

$$-\frac{1}{f_{eq}} = \frac{2(2\mu - 1)}{R}$$

$$f_{\text{eq}} = -\frac{R}{2(2\mu - 1)}$$

For concave mirror, object should be at $2f$ for the image to be at same point

Distance $= \frac{R}{(2\mu - 1)}$

40. Answer (1)

Sol. $P = \sigma \varepsilon A T^4$

$$\frac{P_1}{P_2} = \frac{R_1^2 T_1^4}{R_2^2 T_2^4}$$

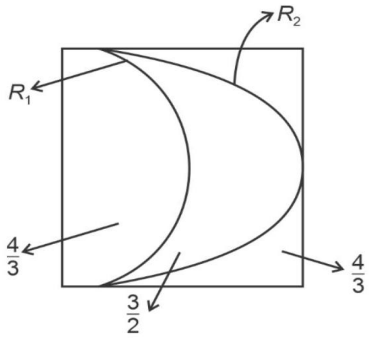
$$\frac{P_1}{P_2} = \frac{1}{16} \times 2^4$$

$$P_1 = P_2$$

$\therefore$ Energy will be same.

41. Answer (2)

Sol.



$$P_{eq} = P_1 + P_2 + P_3$$
$$= \left(\frac{4}{3}-1\right)\left(\frac{1}{R_1}\right) + \frac{1}{2}\left(-\frac{1}{R_1}+\frac{1}{R_2}\right) + \left(\frac{4}{3}-1\right)\left(-\frac{1}{R_2}\right)$$
$$= \frac{1}{3}\left(\frac{1}{R_1}-\frac{1}{R_2}\right) - \frac{1}{2}\left(\frac{1}{R_1}-\frac{1}{R_2}\right)$$
$$P_{eq} = -\frac{1}{6}\left(\frac{1}{R_1}-\frac{1}{R_2}\right)$$

42. Answer (3)

Sol. $F_1 = \frac{GMm}{4R^2}$

$$F_2 = \frac{GMm}{4R^2} - G\left(\frac{M}{27}\right)\frac{m}{\left(\frac{4R}{3}\right)^2}$$

$$= \frac{GMm}{R^2}\left(\frac{1}{4}-\frac{1}{48}\right)$$
$$= \frac{11}{48}\frac{GMm}{R^2}$$
$$\therefore \frac{F_1}{F_2} = \frac{12}{11}$$

43. Answer (2)

Sol. 1 vernier scale division is not always smaller than 1 main scale divisions statement-I is not correct.

Vernier constant = 1 main scale division - 1 vernier scale division

Statement-II is not true

44. Answer (1)

Sol. $\beta = \frac{\lambda D}{d}$

In denser medium $\lambda' = \frac{\lambda}{\mu}$

$\therefore$ β decreases.

45. Answer (2)

Sol. $R_{eq} = (0.5\Omega || 2\Omega) + 0.5\Omega$

$$= \frac{2}{5} + \frac{1}{2} = \frac{9}{10}\Omega$$

$$I = \frac{V}{R_{eq}} = \frac{0.9}{0.9} = 1 \text{ A}$$

SECTION - B

46. Answer (90)

Sol. At $t = 1$

$r_{AB} = -1\hat{i} + (3n+1)\hat{j} + (2-4p)\hat{k}$

At $t = 1$

$v_A = 2\hat{i} + 3n\hat{j} + 2\hat{k}$

$v_B = 2\hat{i} - 2\hat{j} + 4p\hat{k}$

$\vec{v}_A \cdot \vec{v}_B = 0, 4 - 6n + 8p = 0$

$|v_A| = |v_B| \ (3n)^2 + 4 = 4 + 16p^2$

$3n = -4p$

$4 + 16p = 0$

$p = -\frac{1}{4}, n = \frac{1}{3}$

$r_{AB} = -\hat{i} + 2\hat{j} + 3\hat{k}$

$v_A = 2\hat{i} + \hat{j} + 2\hat{k}$

$\therefore L = m\left|\vec{r}_{AB} \times \vec{v}_A\right| = 90$

47. Answer (8)

Sol. $\frac{1}{V} + \frac{1}{U} = \frac{1}{f}$

$$\frac{1}{V} - \frac{1}{24} = 1$$

$$V = \frac{24}{25}$$

$$m = -\frac{V}{U} = \frac{1}{25}$$

$$\left|V_{\text{image}}\right| = m^2 V_{\text{object}} = \frac{1}{25} \text{ m/s}$$

48. Answer (5)

Sol. $U = 60$ m/s

$\theta = 30^\circ$

$t_{H_{max}} = \frac{U\sin\theta}{g} = \frac{60}{10} \times \frac{1}{2} = 3$ s

Height in 1^{st} second $= 30 \times 1 - \frac{1}{2} \times 10 \times 1$

$= 25$ m

Height in last second $= 5$ m

$$\frac{25}{5} = 5$$

49. Answer (4)

Sol. $R = \frac{R_2 R_1}{R_2 - R_1} = \frac{4 \times 2}{2} = 4$ cm

50. Answer (40)

Sol. $R_1 = \frac{2\ell}{k_1 A}, R_2 = \frac{2\ell}{k_2 A}, R_3 = \frac{\ell}{k_3 A}$

$$(100 - \theta)\left(\frac{1}{R_1} + \frac{1}{R_2}\right) = \frac{(\theta - 0)}{R_2}$$

$$(100 - \theta)\frac{(k_1 + k_2)A}{2\ell} = \frac{\theta k_3 A}{\ell}$$

$$(100 - \theta)(k_1 + k_2) = 2\theta k_3$$

$$\theta = \frac{100(k_1 + k_2)}{k_1 + k_2 + 2k_3}$$

$$= \frac{100 \times 180}{450} = 40$$

CHEMISTRY

SECTION - A

51. Answer (2)

Sol. n = 2
Number of stereoisomers = $(2)^2 = 4$

52. Answer (2)

Sol. Both statement-I and statement-II are correct

Statement - I : $CH_3 - O - \overset{\oplus}{C}H_2$ is highly stable carbocation.

Statement - II : Due to hindrance, S_{N2} will not take place easily.

53. Answer (1)

Sol. $q = 0$
$w > 0$
$\Delta U > 0$

54. Answer (1)

Sol. $K_3[Fe(SCN)_6]$ will have CFSE equal to zero $\left(Fe^{3+} : 4s^0 3d^5 \left(t_{2g}^3 e_g^2\right)\right.$

55. Answer (3)

Sol. Electronegativity of AI is higher than that of Mg
⇒ option (3) is correct

56. Answer (1)

Sol. Statement (A), (D) and (E) are incorrect statements.
(A) Propene does not show geometrical isomerism. (A) is incorrect.
(B) (B) is correct.
(C) Dipole moment : cis-but-2-ene > trans-but-2-ene
(D)

DegreeFYD

2-methylbut-2-ene does not show geometrical isomerism. (D) is incorrect.
(E) Trans-isomer has higher melting point than cisisomer. (E) is incorrect.

⇒ (A), (D) and (E) are incorrect.

57. Answer (2)

Sol. $[NiCl_4]^{2-} \Rightarrow Ni^{2+}:4s^0 3d^8$
⇒ No pairing
⇒ sp^3
⇒ Tetrahedral
$[Ni(CO)_4] \Rightarrow Ni^0:4s^0 3d^{10}$
⇒ sp^3
⇒ Tetrahedral

58. Answer (3)

Sol. $CH_3 - C \equiv CH + Na \rightarrow CH_3 - C \equiv C^- Na^+ + \frac{1}{2}H_2$
Statement-I is correct.
Moles of $C_3H_4 = \frac{4}{40} = 0.1$ mole

$$\underset{0.1\,mole}{CH_3-C\equiv CH} + NaNH_2 \rightarrow CH_3-C\equiv C^-Na^+ + \underset{0.1\,mole}{NH_3}$$

Volume of NH3 = (0.1)(22.4) = 2.24 L
Statement-II is incorrect.

59. Answer (1)

Sol. Eu^{2+} and Gd^{3+} have 4^7 configuration.

60. Answer (4)

Sol.

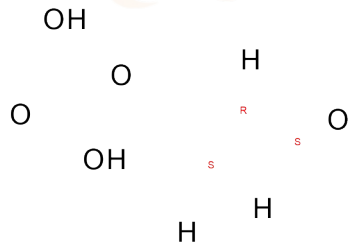
(A) is order of ionic radii. A-(IV)
(B) is correct order of ionisation enthalpy. B-(I)
(C) is correct order of metallic character. C-(II)
(D) is correct order of electronegativity. D-(III)

Option (4) is correct.

61. Answer (1)

Sol. Compound (C), (D) and (E) will give positive Fehling's test.

62. Answer (2)



6-Methoxycarbonyl-2,5-dimethylhexanoic acid.

63. Answer (1)

Sol. $Al^{3+} + 3e^- \longrightarrow Al$

$$\text{Moles of electron} = \frac{2\times 30\times 60}{96500} = \frac{36}{965}$$

$$\text{Moles of Al} = \frac{36}{3\times 965} = \frac{12}{965}$$

Mass of Al $= \frac{12}{965}\times 27$

64. Answer (2)

Sol. For radioactive decay, decay constant does not depend upon temperature because for radioactive decay activation energy is zero.

65. Answer (3)

Sol. $r = a_0\left(\frac{n^2}{z}\right)$

$r = \frac{a_0(2)^2}{(2)}$

$r = 2a_0$

66. 6-Methoxycarbonyl-2,5-dimethylhexanoic acid.

67. Answer (4)

Sol. $H_2S_2O_8$ is obtained by electrolysis of concentrated solution of sulphuric acid.

68. Answer (4)

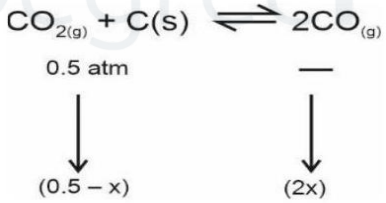
Sol. $\Delta T_b = i(K_b(m))$

ΔT_b order or T_b order

(iv) > (iii) > (i) > (ii)

69. Answer (2)

Sol.



$(0.5 - x) + (2x) = 0.8$

$0.5 + x = 0.8$

$x = 0.3$

$K_p = \frac{(0.6)(0.6)}{(0.2)} = 1.8$ atm

70. Answer (4)

Sol. Vitamin - C is also known as Ascorbic Acid.

SECTION - B

71. Answer (20)

Sol. millimoles of AgCl $= \frac{143.5}{143.5} = 1$

Millimoles of Cl = 1

Mass of Cl $= 35.5 \times 10^{-3}$ gm

% by mass of Cl $= \frac{35.5}{180} \times 100$
$= 19.72\%$
Nearest integer = 20%

72. Answer (45)

Sol. moles of HCl $= 4 \times 10^{-3}$
moles of $Ca(OH)_2$ reacted with HCl $= 2 \times 10^{-3}$
Initial amount of $Ca(OH)_2 = 4 \times 10^{-3}$ moles
Moles of $CO_2 = 2 \times 10^{-3}$
Volume $= 2 \times 10^{-3} \times 22.4$
$= 44.8 \times 10^{-3}$ Lit
$= 44.8\ cm^3$
Nearest integer = 45

73. Answer (6)

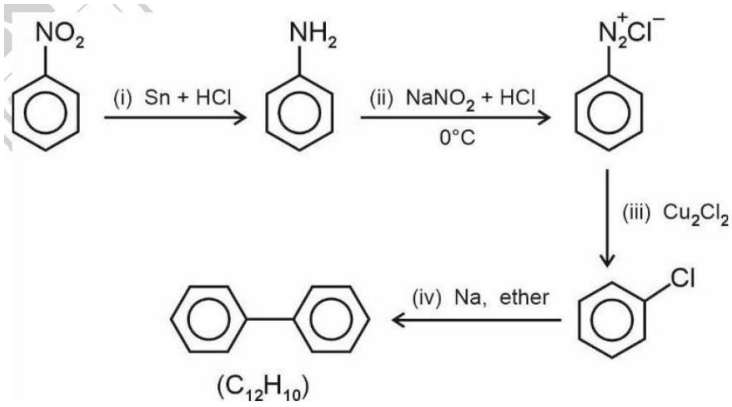
Sol. linear geometry is shown by
$BeCl_2; CO_2; N_3^-; XeF_2; NO_2^+; I_3^-$

74. Answer (69)

Sol. $k = Ae^{-\frac{Ea}{RT}}$
$= \left(10^{20}\right)\left(e^{-\frac{191.48\times1000}{(8.314)(1000)}}\right)$
$= 10^{20}\left(e^{-23.03}\right)$
$= \left(10^{20}\right)\left(10^{-10}\right)$
$= 10^{10}$
$t_{1/2} = \frac{0.693}{10^{10}}$
$= 0.693 \times 10^{-10}$
$= 69.3 \times 10^{-12}$
= 69.3 picoseconds
Nearest integer = 69

75. Answer (154)

Sol.



Molar mass of A $= 154 \frac{\text{gm}}{\text{mole}}$

DegreeFYD